



# TOPOLOGY SEMINAR

## Simplicial distributions and polyhedral geometry

By

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**Abstract:** Simplicial distributions are collections of probability distributions that satisfy certain compatibility conditions that can be encoded topologically using simplicial sets. For a simplicial scenario where the measurement space  $X$  and outcome space  $Y$  are finitely generated the space  $s\text{Dist}(X, Y)$  of allowed simplicial distributions is a convex set, in fact, a convex polytope. By the Minkowski-Weyl theorem of polytope theory it is well-known that there are two equivalent descriptions of a convex polytope as the intersection of finitely many half-space inequalities (H-representation) or as the convex hull of finitely many extreme points (V-representation). In this talk we detail how one constructs the H-representation of  $s\text{Dist}(X, Y)$  and discuss the conversion to its V-representation, known as the vertex enumeration problem. Time permitting, we will also discuss the Bell polytope, which delineates the boundary between contextual and noncontextual measurement statistics, and is a subpolytope of  $s\text{Dist}(X, Y)$ .

**Date:** Monday, Nov 18, 2024

**Time:** 13:30

**Place:** ZOOM

To request the event link, please send a message to [cihan.okay@bilkent.edu.tr](mailto:cihan.okay@bilkent.edu.tr)