



Bilkent University  
Department of Mathematics

## PROBLEM OF THE MONTH

**Term:** February 2016

Find the greatest real number  $T$  satisfying

$$\frac{(x^2 + y)(x + y^2)}{(x + y - 1)^2} + \frac{(y^2 + z)(y + z^2)}{(y + z - 1)^2} + \frac{(z^2 + x)(z + x^2)}{(z + x - 1)^2} - 2(x + y + z) \geq T$$

for all real numbers  $x, y$  and  $z$  such that  $x + y \neq 1, y + z \neq 1, z + x \neq 1$ .